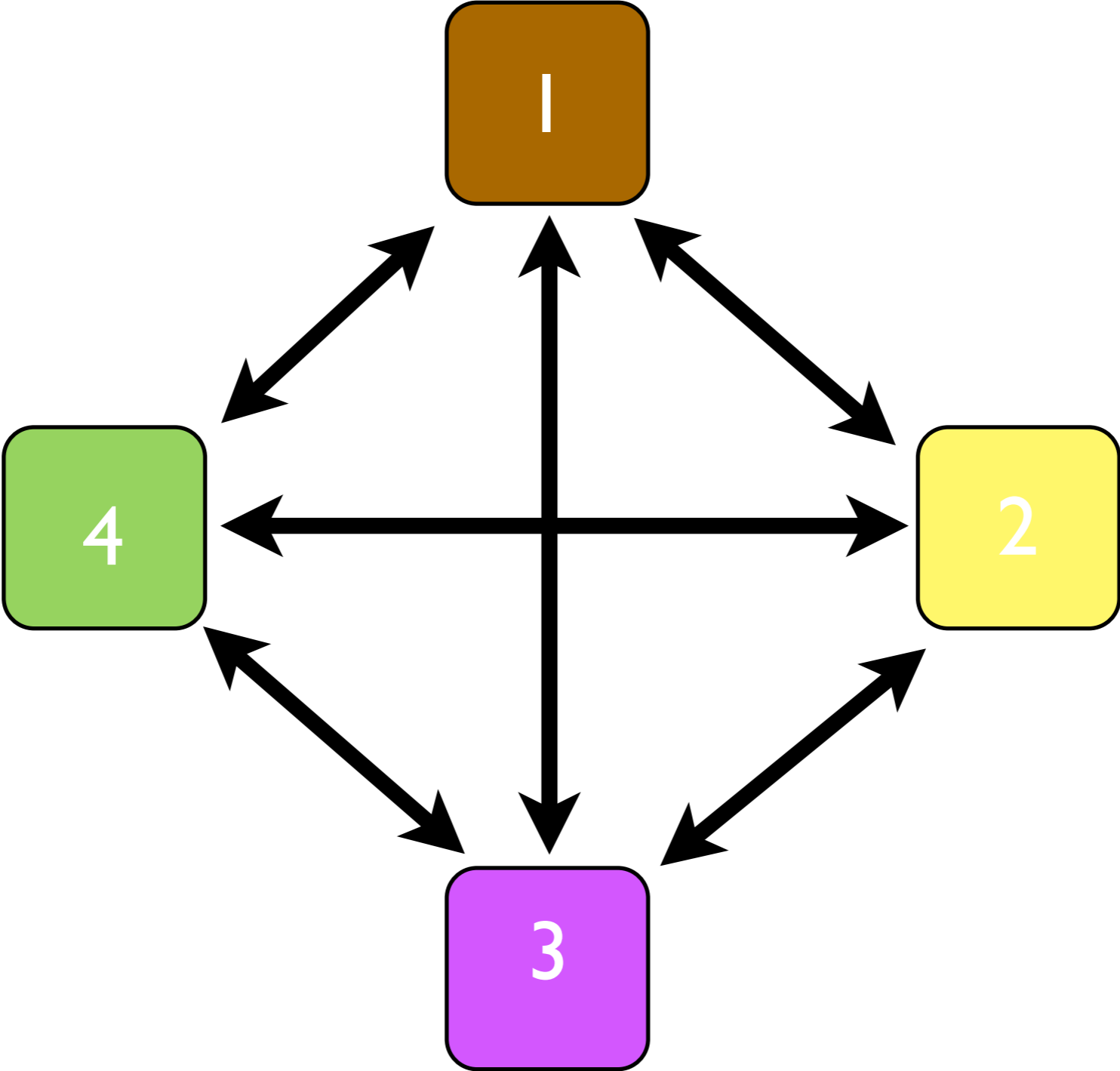
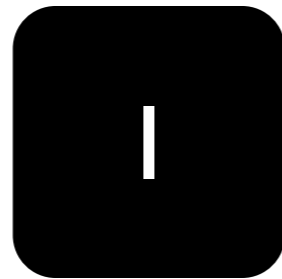
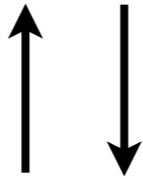
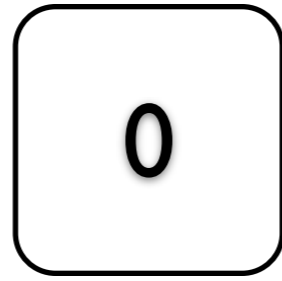


# Modeling Discrete Character Evolution

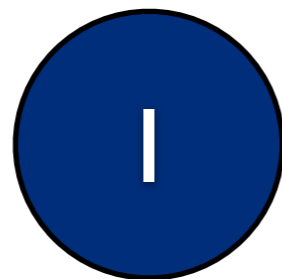
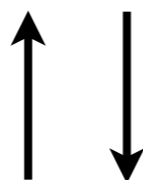
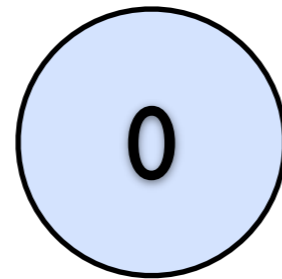


# Consider two discrete characters

- Are they evolving in a correlated fashion?
- When character A changes to state I, is character B likely to change to I as well?

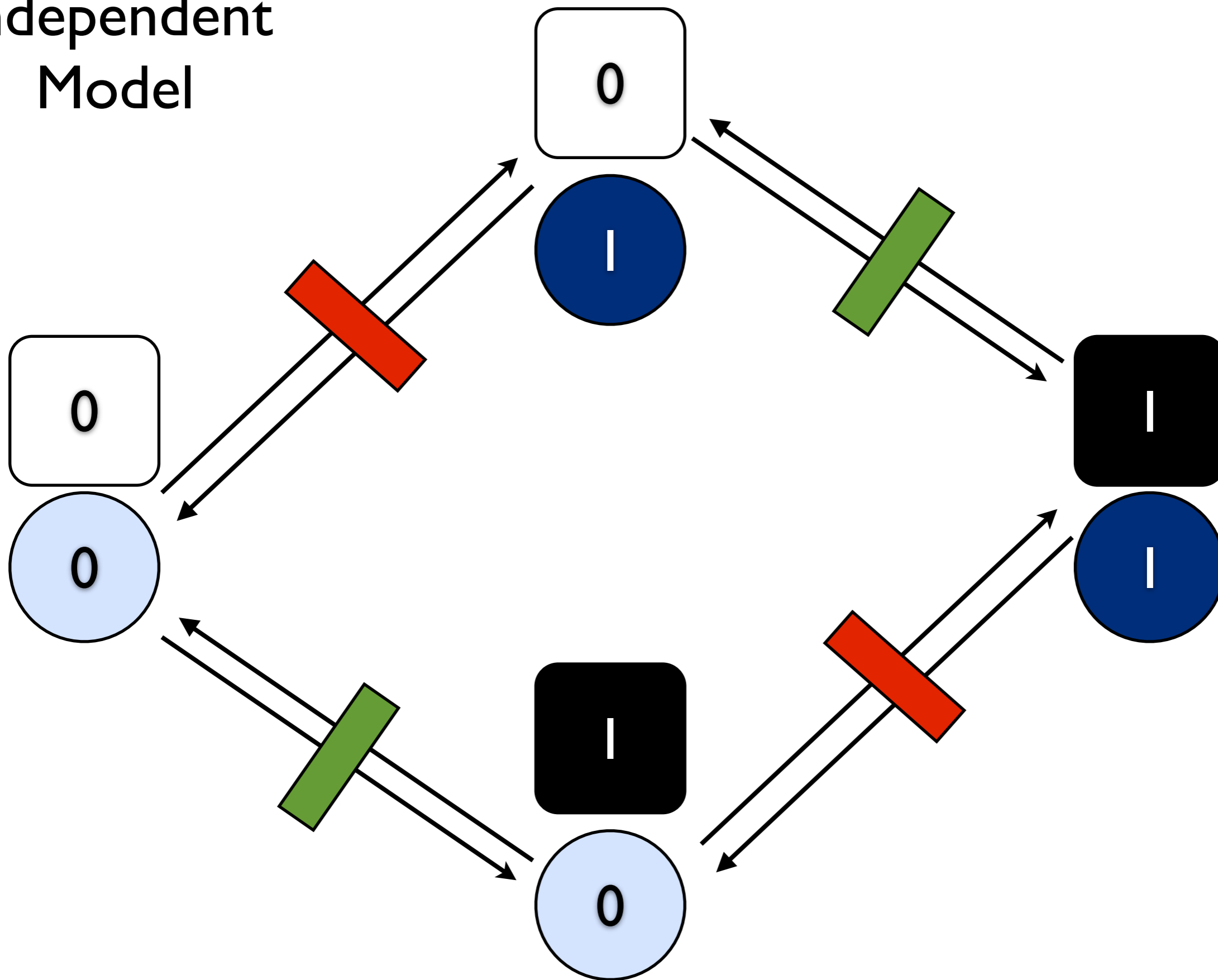


Character 1

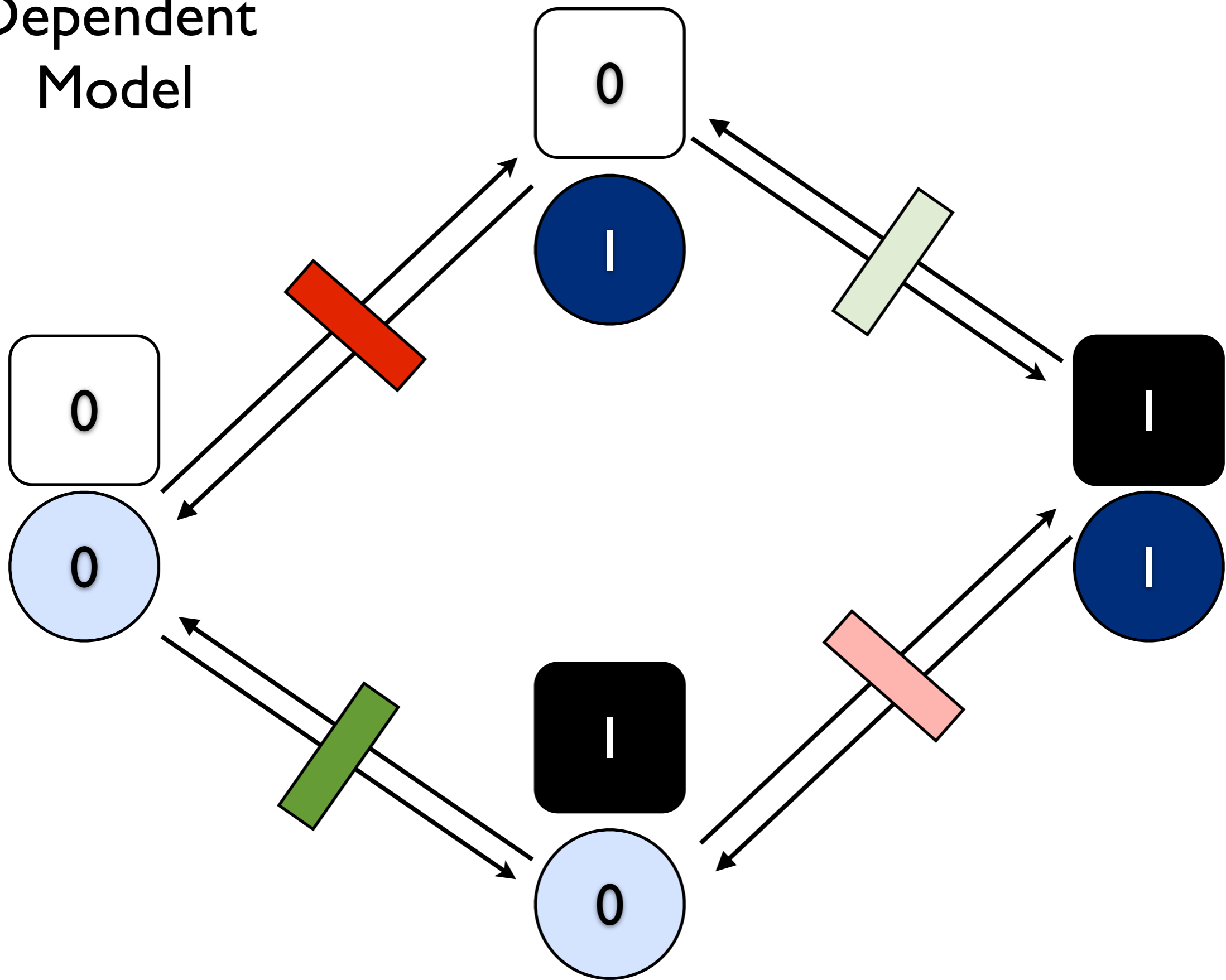


Character 2

# Independent Model



# Dependent Model



# Correlation of Discrete Characters

- Does the rate of change of character 2 depend on the state of character 1?
- Compare models using maximum likelihood

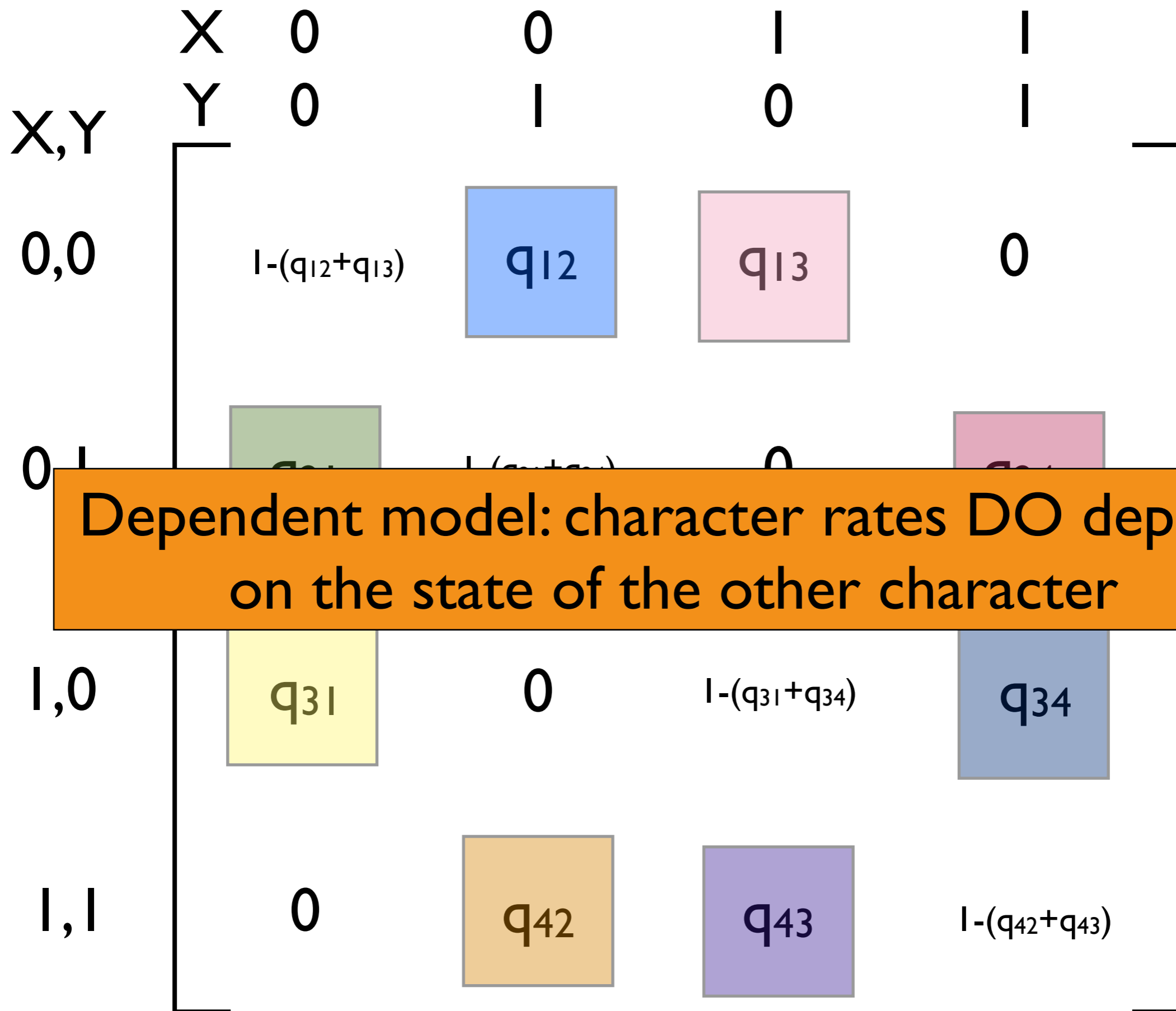
	X	0	0	1	1
X,Y	Y	0	1	0	1
0,0		$1-(q_{12}+q_{13})$	$q_{12}$	$q_{13}$	0
0,1		$q_{21}$	$1-(q_{21}+q_{24})$	0	$q_{24}$
1,0		$q_{31}$	0	$1-(q_{31}+q_{34})$	$q_{34}$
1,1		0	$q_{42}$	$q_{43}$	$1-(q_{42}+q_{43})$



	X	0	0	1	1
X,Y	Y	0	1	0	1
0,0		$1-(q_{12}+q_{13})$	$q_{12}$	$q_{13}$	0
0,1		$q_{21}$	$1-(q_{21}+q_{23})$	0	$q_{23}$
1,0		$q_{31}$	0	$1-(q_{31}+q_{34})$	$q_{34}$
1,1		0	$q_{42}$	$q_{43}$	$1-(q_{42}+q_{43})$

Independent model: character rates do NOT depend on the state of the other character

	X	0	0	1	1
X,Y	Y	0	1	0	1
0,0		$1-(q_{12}+q_{13})$	$q_{12}$	$q_{13}$	0
0,1		$q_{21}$	$1-(q_{21}+q_{24})$	0	$q_{24}$
1,0		$q_{31}$	0	$1-(q_{31}+q_{34})$	$q_{34}$
1,1		0	$q_{42}$	$q_{43}$	$1-(q_{42}+q_{43})$



Dependent model: character rates DO depend on the state of the other character

# Example

- Data on evolution of dewlap color (red, yellow) and perch behavior (high, low) of anoles
- Fit the two models to these data
- Obtain the following results:

# Example

Model	lnL	k	AIC
independent	-132.2	4	272.4
dependent	-125.3	8	266.6